

**Math 356 Assignment 9: Due Wednesday, March 24**

Do the following problems from Part IV of the text

§18: 22,38,41,43,44,45,49

§19: 2,23,26,28,30

§24: 4,10,19

Consider the ring

$$\mathbb{G} = \{a_1 + a_2i + a_3j + a_4k : a_1, a_2, a_3, a_4 \in \mathbb{Z}_5\}$$

with addition and multiplication defined as for the Quaternions, i.e., by the formulas on pp. 225 of the text. Show that  $\mathbb{G}$  is *not* a division ring, by finding a nonzero element which is not a unit. (See Theorem 24.10 of the text for a general result along these lines.)